

Master Thesis

**Multi-Asset Factor Investing**

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## **Abstract**

In this paper, the performance of three factor investing strategies for U.S. market is being explored. According to financial studies, low-volatility-, value- and momentum strategies have proven to generate systematic yield across various asset classes. However, the literature on this topic is inconclusive about the effect of each factor investment strategy on a multi-asset portfolio. Unlike previous studies, this paper focuses on examining the impact of factors on a multi-asset portfolio, consisting of equities, corporate investment bonds, high-yield bonds, commodities and REITs. This study builds on the current financial literature by using more recent dataset 1990-2015, along with analyzing factor strategies both per individual asset classes, as well as combined in a multi-asset portfolio. The results indicate that low-volatility, value and momentum strategies can be beneficially exploited for both the multi-asset portfolio and individual asset classes. The multi-asset portfolio has generated the highest alpha spread and Sharpe ratio when exploiting low-volatility strategy. For value and momentum strategies, REITs have outperformed the Sharpe ratio of the multi-asset portfolio. Additionally, robustness checks proved that the financial crises had an impact on the yields across individual assets and on the multi-asset portfolio.

**Keywords: factor investing, multi-asset portfolio, equities, bonds, commodities, REITs**

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## **Section I: Introduction**

Nowadays, an increasing number of investors are hunting for systematic yield. In the 1970s researchers questioned the conventions of the CAPM model that assumes rational markets and investors, and forecasts positive linear relationship between risk and return. One of the first who investigated stock` yields and established that the relationship between risk and return is not linear are Treynor, 1962, Sharpe, 1964, Black, 1972. Contrary to the fundamental CAPM theory market risk does not fully explain all stock performance, but other factors do so. Fama and French, 1996, acknowledged the presence of asset pricing anomalies and conclude that small- and value stocks produce higher returns.

Present empirical work has proved that investing based on particular features of assets, also referred to as ‘factor investing’, may lead to greater risk- adjusted returns (Asness, Markowitz and Pedersen, 2013). A fascinating market phenomenon is the value effect which represents the relation between an asset’s return and the ratio of its book value relative to its current market value. The overview of factor investing could very well continue with Jegadeesh and Titman who verified that buying stocks that have performed well in the past and selling stocks that have performed poorly in the past could lead to excess return. This phenomenon is now accredited as the momentum effect. Momentum investing is ‘a lively game of hot potato - buying rapidly appreciating stocks, holding them for a relatively short period, and selling them before their price trends reverse direction.’ (Larson, 2013). Asness, Moskowitz and Pedersen, 2013, establish that value and momentum effect occur across globe and asset classes. Blitz and Van Vliet (2007) further contribute to the factor investing literature and provide empirical evidence that stocks with low volatility produce high risk-adjusted returns. This effect is now known as the volatility effect and it has been proven to be present across the U.S., European and Japanese markets. Besides, Blitz and Van Vliet also proved that size and value effect are not the reason why the volatility effect occurs. They argue that investors should treat low risk stocks as a distinct asset class in the asset allocation phase, in order to exploit this anomaly in practice.

Based on the aforementioned academic studies, it can be summarized that by allocating to value, momentum and low volatility factors, systematic excess return can be reaped. Attracted from the

upside potential from factor investing, experts started exploiting these market anomalies by transforming them into investment strategies, which have led to the evolution of factor investing. However, there is a lack of consent on what factor investing really is and what distinguishes it from the traditional quantitative investment methods. Factor investing is a systematic approach to investing strategically in specific parts of the financial markets which generate better returns over longer periods than those in other sectors. According to the financial literature, factor premiums have been proven to be robust over time. Such premiums have been also observed in the multi-asset space. Therefore, factor investing could be exploited not only for stocks but could potentially be taken advantage of in other asset classes.

Now, it is well known that with stock pitching an investor faces the risk of under diversification, hence making him/her exposed to a substantial idiosyncratic risk. The literature on market anomalies mainly examines factors individually. Inspired by these studies, this paper contributes to and extends the existing factor investing literature in several ways. First, it fills the literature gap by comparing the performance of the different factors on multi-asset portfolio, as this offers diversification benefits for investors. Second, it produces robust empirical estimates of the alpha spread for momentum, total volatility and value. Lastly, this study utilizes a portfolio based regression approach, inspired by Fama and French (1996), to examine the excess return that can potentially be achieved and analyzes relatively recent data (1990-2015) across the U.S. market.

The main goal of this research is to analyze whether an investment strategy based on the value, momentum and low-volatility anomaly is worthwhile. Consequently, this paper will aim to prove a consistent excess return premium that can be achieved if the above-mentioned market anomalies are put into practice.

The remainder of this paper is organized as it follows: Section II documents relevant literature on the risk-return relationship. Section III elaborates on the data collection procedure and formulates the research questions, while section IV describes the methodology. Next, Section V delivers the results and the corresponding implications. Additionally, Section VI addresses robustness checks. Finally, Section VII is centered on concluding remarks.

## **Section II: Literature review**

Researchers have found that market anomalies (referred to as factors in the above section I.) are responsible for a large portion of the market outperformance. Consequently, factor investing is attracting higher attention as an effective investment model and a growing number of institutions have shifted their attention from a traditional asset allocation approach towards a factor allocation approach. As a result, diversification occurs by allocating to different factor premiums that have superior risk/return profiles than market-capitalization weighted indices. Some of the most widespread factors in this respect are value, momentum and low-volatility. Therefore, it is important to analyze the impact of each of these factors on a multi-asset portfolio as this might offer not only diversification benefits to investors, but also greater yield and Sharpe ratio.

As mentioned above, important market anomalies that are exploited for stocks are the value premium (Fama and French, 1992), the size premium (Banz,1981), the momentum premium (Jegadeesh and Titman, 1993) and the low-volatility premium (Blitz and van Vliet,2007). However, factor premiums have a larger presence also elsewhere rather than just within equities. They can be found in other asset classes such as bonds and commodities (Asness, Moskowitz and Pedersen, 2009), while the low volatility effect could be taken advantage of in credits (Houweling et al.,2005). When taking into consideration all factor premia, momentum is considered one of the most attractive and is in most cases part of every equity` factor investment strategy, mainly because of its low correlation with factors like low volatility and the fact that it can have a negative correlation with value. Consequently, investors tend to hedge their portfolios against reversal risk (‘winner’ stocks to become ‘loser’ stocks) that might occur with momentum investing strategy and minimize the related transaction costs, by combining momentum with other factors. When it comes to corporate fixed income market- size, low-risk, value and momentum factors have economically meaningful and statistically significant risk-adjusted returns. Besides, Houweling, 2014, shows that in a multi-asset framework, allocating to corporate bond factors has generated returns beyond the ones from allocating to equity factors.

Before it is proceeded to the in-depth literature review of the above-mentioned factors, it is

important to discuss the fundamental Capital Asset Pricing Model, which serves as a stepping stone in the finance literature. Grounded on the portfolio theory from Markowitz (1959), CAPM is a theoretical model that assumes that the expected return on a stock is only dependent on its systematic risk (Sharpe, 1964, Lintner, 1965). However, the theory of CAPM and what happens in reality are in big contrast. The following paragraphs will elaborate more on the CAPM model, followed by an overview of the literature on factors.

Sharpe (1964) `s and Lintner (1965) `s CAPM method tries to explain how to evaluate risk, as well as its connection to the expected asset `s return. Berk and DeMarzo, 2014, highlight the three main assumptions of the CAPM model, to evaluate its effectiveness. First, all investors have identical outlooks concerning the expected return of the assets, their correlations and volatilities. Second, investors can borrow and lend at the risk-free interest rate, in addition to trade all assets at market price. The third postulation is that investors keep only such portfolios that generate the greatest expected yield for a given level of risk. However, Fama and French, 2004 prove that these assumptions of the CAPM are not representative for the whole market. As explained in the introduction section, Black, 1972, Lucas, 1978, Fama and French, 1992, Barberis et al., 2015 establish that market anomalies are present and are founded based on CAPM. For instance, Russel and Thaler, 1985, De Long, 1990, find a mismatch between reality and CAPM assumptions. When studying investors behavior, the authors find that investors are not entirely rational.

Furthermore, De Bondt and Thaler, 1994, presents the concept of irrationality among investors (Shleifer, 2000) and how more sophisticated investors can benefit from exploiting the market anomalies that might occur because of this behavioral bias. For instance, Daniel, Hirshleifer and Subrahmanyam, 1998, Barberis, Shleifer and Vishny, 1998, show that investors can either overreact or underreact (Hong, Stein, 1999, Chan, Jegadeesh and Lakonishok, 2006) to unexpected events or news, which can cause momentum outcome. From the studies of Daniel, Hirshleifer and Subrahmanyam, 1998, Barberis, Shleifer and Vishny, 1998, Hong and Stein, 1999, it can be summarized that the overreaction or underreaction can be mainly caused by lack of analyzing capabilities, overconfidence, self-attribution, conservatism bias, or loss aversion. Value and momentum anomalies could also occur due to flows between the investment capitals (Vayanos and Woolley, 2012). Additionally, momentum anomaly could also occur because of collective

managers' behavior, also referred to as 'herding' behavior (Dasgupta, Prat, and Verardo, 2011) as managers that are in a group can take collective decisions without a specific direction. Hence, this can cause an investment biased decision.

On the other hand, the rationality of CAPM is also investigated by Jagannathan and Wang, 1996 who prove as well that the model does not measure entirely the risk and does not cover the complete relationship between risk and expected return. Other financial studies such as Faff, 2004, also prove that the three-factor model explains better the risk-return relationship than the traditional CAPM model (Gaunt, 2004). Eraslan, 2013, states that the model that builds on CAPM, namely the Fama and French three-factor model, captures the CAPM inefficiencies by incorporating factors in their methodology.

#### **i. Low-Volatility**

There is a broad arsenal of studies that has analyzed the low-volatility anomaly and has shown that contrary to CAPM methodology, excess return can be achieved. Research on this anomaly can very well start with Falkenstein, 1994, who found out that the relationship between expected asset's return and risk has proven to be flat, or even negative, which means that CAPM expectations do not hold. Later, Ang et al., 2006, conclude that higher risk is not necessary compensated with higher return. In the same period, Ang, Hodrick, Ying, and Zhang, 2006, explain that this means that low-risk stock investments should outperform high-risk stock investments. Based on the observations, recent empirical research focused on analyzing whether low-risk stocks indeed outperform the high-risk stocks. Baker and Haugen, 2012, examined the length of this anomaly, and the yield differences it generates among various industries and concluded that is robust over time. Going into more details, Baker, Bradley and Wurgler, 2011 prove that the anomaly holds even if different risk interpretations are considered, namely low beta, or volatility (as a low volatility anomaly) as a substitute for risk.

Low-volatility anomaly could be explained through both rational and behavioral theories. Some of the rational theories include shorting constraints and leverage constraints. Institutional investors, for example, are constrained in the amount of leverage they can take on and this explains the low



yields on the high-risk assets (Frazzini and Pedersen, 2014). Besides, investors could also face shorting constraints, hence, if they would like to short on high-volatile asset and long on low-volatility ones, this might not be allowed. In case that there are no shorting constraints and all investors are to behave rationally and trade on the low-volatility anomaly, the phenomenon is likely to disappear. However, this cannot happen in practice as investors do not behave in the same way. On the other hand, when we look at the behavioral explanations of this anomaly, the concept of lottery disposition (Kahneman and Tversky, 1979) might apply. The authors demonstrate that when people should make a choice between a low chance of a significant gain and a high chance of small loss, they will rather go for the riskier option. Kumar, 2009, Barberis and Huang, 2008, Bali, Cakici and Whitelaw, 2011, also confirm the theory that investors are likely to take on the hazard of investing in high volatility stocks as they will be exposed to a chance of earning excess return. Furthermore, Baker, Bradley and Wurgler, 2011, explain that overconfidence bias might cause investors to stick to their initial strategy, because they feel overconfident in their analysis. Additionally, Baker, Bradley, and Wurgler, 2011, state that irrational investors tend to evade low risk stocks and tend to pay more for hazardous stocks.

To test whether low-volatility strategy could generate excess return, researchers deploy relatively similar statistical methods. Initially, stocks are sorted based on volatility levels and then allocated to equally weighted portfolios. Every month each portfolio is being rebalanced. CAPM` and Fama and French three-factor model` alphas are attained within each quintile or decile of the equally weighted portfolios.

## **ii.    Value**

Value effect is present across most asset classes, thus is one of the most implemented factor investing strategies (Asness, et all, 2013). Basu (1977), Rosenberg, Reid, and Lanstein (1984) show that strategies based on book-to-market ratios have produced excess returns over a long-term period (De Bondt and Thaler (1985, 1987)). In line with Merton (1973), Fama and French, 1992, also demonstrate that the excess return occurs as a compensation for risk. On the contrary, Lakonishok, Shleifer, and Vishny,1994, argue that there is little evidence that high book-to-market ratio and high cash-flow-to-price stocks are riskier based on traditional concepts of systematic risk. For

diverse reasons, Lakonishok, Shleifer, and Vishny, 1994, conclude that value stocks have been underpriced relative to their risk and return. Daniel and Titman, 1996, also state that value stocks deliver excess return because it takes time for the markets to realize that earnings growth rates for value stocks are higher than initially expected and opposite to attractive stocks. In addition, LaPorta, Lakonishok, Shleifer, and Vishny. 1997, show that significant portion of the return difference between value and attractive stocks is because of earnings surprises that are systematically more positive for value. Moreover, Piotroski, Joseph, 2000 test that when using a simple check based on historical financial performance, investors can indeed earn abnormal return by creating strong value portfolio. Based on the financial literature it can be summarized that empirical evidence proves that the value effect is significantly strong, no matter the reason why strategy works in practice (Asness, 1997).

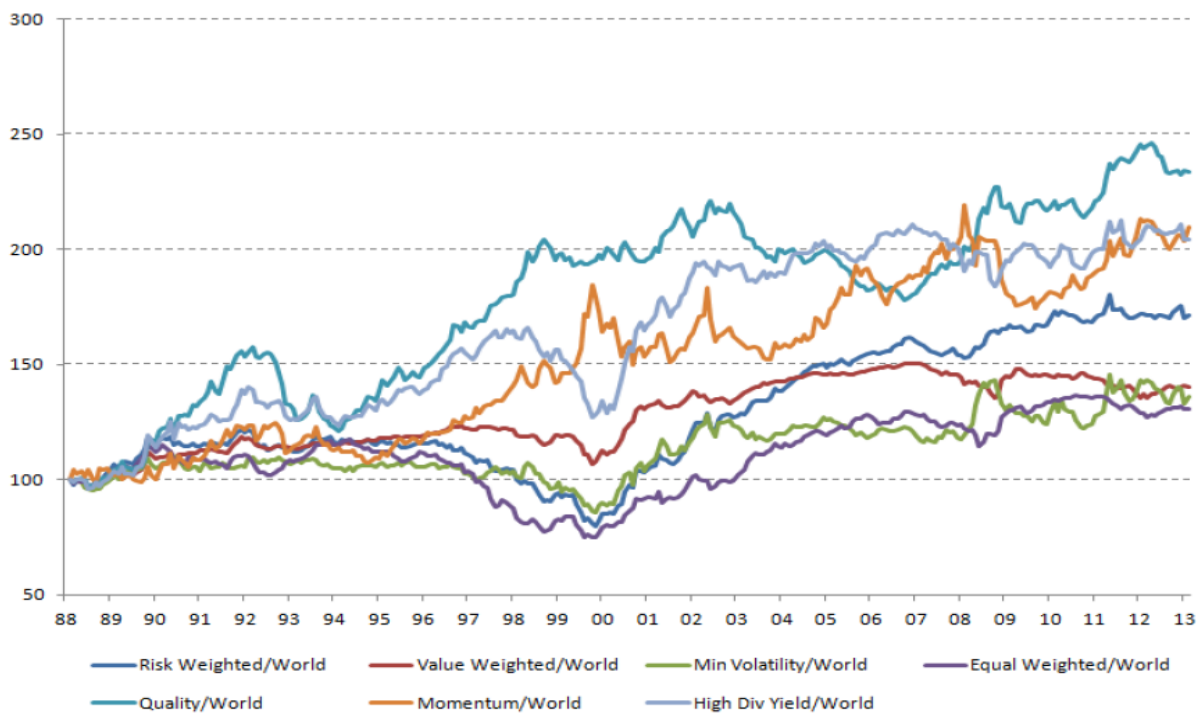
### **iii. Momentum**

The momentum anomaly is one of the most widely studied phenomenon in capital markets. Among the first studies of the momentum effect was conducted by Levy (1967), who found that significant abnormal returns are generated by holding stocks with higher than average prices over the recent past period. Later, Jegadeesh and Titman (1993) also established that past winners in the U.S. capital markets outperform previous losers. The research of Jegadeesh and Titman (1993) ranked each month the returns of companies over the past 6 months. Decile portfolios were formed based on these rankings, where the top decile is called 'winners' and bottom decile is called 'losers'. Jegadeesh and Titman (1993) documented that above 10% average excess return per year could be achieved by using 6 months of past return. Going more in-depth, Asness (1997) concluded that winners become losers and losers become winners over the long-term. Pursuing the methodology by Jagadeesh and Titman (1993), Rouwenhorst (1998) found similar outcome for the European market. However, researchers have established that for the last hundred years there have been several periods during which the returns from winning stocks have totally crashed. Momentum premium could drop significantly, impacting severely the profits of investors (Cooper, Guitierrez and Hameed (2004). Other studies such as Sun and Stivers (2010) show as well that momentum is procyclical, especially in periods such as the recent financial crises. Based on the aforementioned risks that momentum strategy carries, risk-averse investors might dislike momentum investing. On

the other hand, hazardous investors would like to take on this risk and through a well-diversified factor portfolio to manage to hedge the possibility of a reversal risk. Barroso and Santa Clara, 2013, also show that in hand with its extraordinary performance, momentum might also sporadically crash (Daniel and Moskowitz, 2014). Therefore, it is necessary momentum risks to be hedged by incorporating value effect in investors' portfolios (as explained above), due to the negative relationship between these two factors.

Referring to the above paragraph that mentions factor cyclical, it is important to describe what it means in practice. Factor indices have demonstrated that 'excess risk adjusted returns over long time periods' have exhibited 'significant cyclical which sometimes includes periods of underperformance' (Bender, 2013). Exhibit 1 below shows that some of the factor indices exhibited 2-3 years of underperformance for the period 1988-2013. Hence, for a factor investing strategy to work, an investor should consider a long-term strategy. Therefore, only a long-term investor could be able to exploit this investment approach as investors with shorter horizons would not be able to benefit from the full cycle required for factor investing to generate excess return.

Exhibit 1: All systematic factors are cyclical (cumulative returns, June 1988 to June 2013)



Source: [https://www.msci.com/documents/1296102/1336482/Deploying\\_Multi\\_Factor\\_Index\\_Allocations\\_in\\_Institutional\\_Portfolios.pdf/857d431b-d289-47ac-a644-b2ed70cbfd59](https://www.msci.com/documents/1296102/1336482/Deploying_Multi_Factor_Index_Allocations_in_Institutional_Portfolios.pdf/857d431b-d289-47ac-a644-b2ed70cbfd59)

## **Section III: Data and Research Questions**

### **i. Data**

#### *Equities*

The examined period in the study covers the period January 1990 to December 2015. The daily adjusted closing prices expressed in U.S. dollars of equities of the United States are gathered from Thomson Reuters DataStream. SandP500 index is used and in the analysis monthly stock prices are utilized.

The risk-free rate and the factors - market, size, value, and momentum - are provided by the Kenneth French data library. In the financial literature, this is a common proxy for the risk-free rate (Bollerslev, Engle and Wooldridge, 1988). Consequently, for the risk-free rate the one-month U.S. Treasury bill (T-bill) rate is applied.

#### *Bonds*

For the period January 1990 to December 2015, survivorship-bias free data of the Barclays U.S. Corporate Investment Grade index and the Barclays U.S. Corporate High Yield index are collected from DataStream. Barclays provide various full characteristics of each bond in each month (Houweling, 2014). To estimate the factor portfolios, the excess return of a corporate bond versus duration-matched Treasuries is used. Barclays offers also these excess returns. (Houweling, 2014).

#### *Commodities*

Commodity prices and returns are obtained from data stream covering the U.S. market. Examined period covers also the beginning of 1990 to the end of 2015. Going into more details, SandP GSCI Commodity total return (OFCL) index is downloaded. For consistency with the data gathering process of the variables, only monthly data is collected.

## REITs

REIT's data is collected from the Center for Research in Security Prices (CRSP)/ Ziman Real Estate Database. The used data frequency is monthly and the chosen period is as well 1990 to 2015.

### **ii. Research Questions**

This paper will aim to investigate the following research question:

*Which factor investing strategy generates the greatest yield on a multi-asset portfolio?*

Research Sub-Questions:

- Which factor investing strategy will generate the highest yield per asset class?
- Which factor investing strategy will generate the biggest yield for the multi-asset portfolio?
- Is the multi asset portfolio's Sharpe ratio greater than the one of per asset class?

The above questions give an indication of what answers could be found in the results section of this study.

## **Section IV: Methodology**

### **Low-volatility**

The Center for Research in Security Prices (CRSP), the monthly returns from 1990 to 2015 for all stocks traded on NYSE, NASDAQ and AMEX are taken. Then, the monthly volatility is calculated in the same way as in Blitz and Van Vliet (2007). Excess returns are calculated by deducting the risk-free rate, measured by the short-term interest rate, taken from the Kenneth French database.

All portfolios are updated on a monthly basis and at the end of each month, stocks are being ranked on the past 6-month volatility of returns, following AN et al., (2014). Subsequently, equally-weighted quintile portfolios are constructed based on these rankings. Stocks with the lowest (highest) volatility are assigned to quintile one (five). Afterwards, the (excess) mean return is calculated for each portfolio. These portfolios have a holding period of 1 month, after which the portfolio is rebalanced. The obtained time-series of the five portfolios will be utilized in the regression analysis to estimate the alpha of each portfolio. The CAPM and the Fama and French 3 factor model are implemented as a benchmark.

Furthermore, a slightly different approach is undertaken for the multi-asset portfolio construction. The asset classes are first ranked according to their individual volatility periods and only then the multi-asset portfolio is formed based on the per asset`s volatility rankings. Additionally, different volatility periods per asset class will be first analyzed so that it can be explored on which volatility window each asset generates the highest Sharpe ratio. Based on this analysis, the multi asset portfolio will be constructed by taking the most efficient combinations of volatility periods per asset class.

## **Value**

As in most financial literature, equities are being sorted on their book to market value, following the approach of Fama and French (1992) and Lakonishok, Shleifer, and Vishny (1994). For all other asset classes, the methodology of Asness, Moskowitz and Pedersen (2013) will be followed. As ‘uniformity across asset classes is difficult to be achieved, a rather simple and consistent measures of value will be used’. (Asness, et all, 2013). For bonds, the 5-year change in the yields of investment-grade and high-yield bonds will be computed. The result will be like the negative of the past 5-year return on these bonds. (Asness, et all, 2013). For commodities, value is estimated as the log of the spot price 5 years ago, divided by the most recent spot price. (Asness, et all, 2013). Consequently, the negative of the spot return over the last 5 years is utilized (Asness et all, 2013). Unfortunately, the paper of Asness, 2013, does not consider REITs, therefore this study will build on the paper ‘Value and Momentum everywhere’ (Asness, et all, 2009) by also investigating value effect on REITs. This will also be tested by replicating the aforementioned methodology.

Consequently, according to the asset's value, ranks will be assigned and quintile portfolios will be formed (by following the method of the low-volatility investment strategy). Thereafter, excess returns are calculated with the purpose of estimating the per asset class's pricing error of each regression.

## **Momentum**

To measure momentum, the simplest and most commonly used measures are utilized. This paper's goal is to maintain a simple and fairly uniform approach that is consistent across asset classes' (Asness, Moskowitz, Pedersen, 2013). This study implements a simple portfolio-based regression methodology to analyze the momentum effect. To do so, momentum portfolios are formed for equities, investment-grade-, high-yield- bonds, commodities and REITs. Going into more details, strategy based on cumulative returns of 12 months and strategy based on cumulative returns of 6 months will be deployed with the purpose of testing which one generates the highest yield per asset class. At the end of each month, the asset classes are being ranked on their cumulative returns, following Jegadeesh and Titman, 1993. Subsequently, equal-weighted quintile portfolios are created based on these rankings. Stocks, bonds, commodities and REITs with the highest (lowest) cumulative returns are assigned to the top (bottom) quintile. Subsequently, the (excess) mean return is calculated for each portfolio. Following the approach of low-volatility and value strategies, the portfolios also have a holding period of 1 month, thereafter being rebalanced. Most of the analysis are focused on the zero-investment portfolio that is calculated by taking the difference in returns per month between quintile 5 and quintile 1. The obtained time-series will be utilized in the regression analysis to estimate the pricing error of each portfolio against the two benchmark models mentioned above, namely the CAPM and Fama and French 3 Factor model.

## **Construction of the Multi-Asset Portfolio**

Before creating the multi-asset portfolio, regressions will be first run per asset class and per factor. Thereafter, a combined portfolio consisting of equities, bonds, commodities and REITs is constructed and the regressions are applied per factor on the multi-asset portfolio. Therefore, it is important to explain the formation of the portfolio. The return of the multi-asset portfolio is

computed by utilizing the bellow formula:

$$E(R) = w_1R_1 + w_2R_2 + \dots + w_nR_n$$

where 'E(R)' is the expected return of the multi-asset portfolio, 'w' indicates weight per asset class and 'R' indicates the return of an asset. Hence, the combined portfolio consists of 70% return on equities, 10% return on combined bond portfolio return (50% weight in high yield bonds and 50% weight in investment grade bonds), 10% return on commodities and the remaining 10% return on REITs. The below formula shows in detail the weights per asset class for the multi asset (MA) portfolio:

$$\text{MA portfolio return} = 70\% * R_e + 10\% * R_b + 10\% * R_c + 10\% * R_r$$

where  $R_e$  stands for return on equities,  $R_b$  stands for total bonds portfolio return, consisting of 50% investment grade bonds and 50% high-yield bonds.  $R_c$  represents return on commodities, while  $R_r$  is return on REITs. After the multi-asset portfolio return is computed, rankings are assigned as per the above-mentioned methods. For momentum, two versions of cumulative returns of the portfolio are being tested (cumulative returns 6- and 12 months), to check for different scenarios of when the multi-asset portfolio generates higher return and substantial alpha spread. Subsequently, equally-weighted quintile multi-asset portfolios are created based on these rankings. Multi-asset portfolios with the lowest (highest) rank are allocated to quintile one (five). The rank depends on which factor investing strategy takes place. As discussed in the above paragraphs, it is either sorted on volatility periods for low-volatility strategy, value for value strategy or cumulative returns when it comes to momentum. Afterwards, the (excess) mean return is calculated for each portfolio. Alpha-spreads are computed after the regressions on CAPM and 3-factor Fama and French model are performed. Here, as explained in the low-volatility methodology, it is useful to mention again that for the low-volatility strategy, before the multi-asset portfolio is constructed, volatility periods per asset class are first defined and ranked, and only thereafter the multi-asset portfolio is formed.



## **Section V: Empirical Results**

As outlined in the methodology part of this paper, to test for the factor strategies across different asset classes, cross-sectional regressions are run based on CAPM and Fama and French 3 factor models. For each factor investing strategy, regressions are first run per asset class, namely equities, investment grade bonds, high- yield bonds, REITs and commodities. The second step involves constructing a multi-asset portfolio of these asset classes and analyze the effect of each anomaly on the whole portfolio. The results below are presented in subsections that primarily indicate the factor investing strategy and next the asset class. Here, it is important to highlight that for the all analyzed investment strategies, the multi-asset portfolio consists of the following weights: 70% equities, 10% bonds, 10% commodities and 10% REITs.

### **i. The low volatility anomaly**

Cross-sectional regressions are first run based on CAPM and second on Fama and French 3 factor models, with the aim of testing the low-volatility anomaly across different asset classes. As outlined in the above section, individual asset classes are first ranked according to their volatility periods and only then the multi-asset portfolio is constructed.

#### **Equities**

Table 2 presents factor loadings of the CAPM and Fama and French 3 factor models that are regressed on quintiles sorted on the 6-month and 12- month return volatility of equities. Jensen's alpha across the portfolios show a significant positive effect on the excess return which indicates that low volatility stocks generate excess return. In line with the empirical evidence, the alphas of the portfolios increase from the first to the fifth quintile portfolio. The same observation has been found when re-testing for the low volatility anomaly with respect to the CAPM. Furthermore, it is important to look at the alpha spread which is the spread between the alphas of quintile 5 (P5) and quintile 1 portfolios (P1). When analyzing the effect per equally weighted portfolios, it can be summarized that P1 shows a significant lower alpha relative to the one of P5, which indicates positive alpha spread and that the higher the volatility of stocks, the worst the performance on the

excess return, which is inconsistent with the CAPM theory, but coherent with previous research (Blitz and Van Vliet, 2007, Baker, Bradley and Wurgler, 2011). The results on SMB and HML for equities indicate that the value premium, and the size premium have a positive, however, insignificant impact on the alpha spread. An interesting observation is that when equities are sorted on 12 months volatility period, the alpha spread seems to increase, hence the bigger the volatility period, the better performing the low-volatility strategy. Finally, Sharpe ratio of equities sorted on 6 months volatility is 0.023 and it is slightly lower than the Sharpe ratio of equities sorted on 12 months volatility (0.027) (table 11). Hence, it can be concluded that the higher the volatility window, the higher the excess return generated from the low-volatility strategy and the higher the Sharpe ratio.

#### Investment grade bonds

Unlike any other studies on this topic, low volatility anomaly has not been explored on the fixed income market. Low-risk strategy has indeed showed that work on this asset class. However, this paper tries to fill the literature gap and test whether low-volatility anomaly can generate excess return. From table 2 it can also be concluded that investment grade bonds also generate positive excess return. The results hold for both CAPM and Fama and French 3 Factor model. However, the insignificant SMB and HML factors prove that the size premium as well as the value premium do not contribute to a positive effect on the excess return. Hence, size and value effect do not seem to work for this asset class. When analyzing investment grade bonds, factor loadings of the Fama and French 3 factor model are as well regressed on quintile portfolios but this time this asset class is analyzed by sorting it on the 12-months and 18-months return volatility. Table 2 indicates that higher alpha spread is achieved for investment bonds sorted on 18 months. The same results have been obtained when examining for the low volatility anomaly with respect to the CAPM. Sharpe ratio for investment bonds sorted on 18 months is higher than for these sorted on 12 months (table 11), however, equities generated higher Sharpe ratio than this asset class.

#### High-yield bonds

Following the identical abovementioned approach, the effect of low-volatility investment strategy on high-yield bonds lead to the same conclusions as for the investment grade bonds. Table 2 outlines the CAPM results as well as the Fama and French 3 factor model. Identically to the investment grade bonds SMB and HML proved to be insignificant. In line with investment grade

bonds, high-yield bonds sorted on 18 months generate higher alpha spread and higher Sharpe ratio (table 2 and 11 respectively). Consequently, based on results for investment grade bonds and high-yield bonds it can be summarized that this anomaly could be exploited to deliver positive excess return for this asset class.

### Commodities

Moving to commodities, factor loadings of the Fama and French 3 factor model are as well regressed on quintiles, however, for this asset class different volatility windows are applied. At first the effect of quintiles sorted on the 6-month return volatility of commodities turned out to be insignificant. To prove that this strategy works for commodities as well as for equities, bigger volatility period is used. The outcome was retested for portfolios sorted on 12-, 18-, 24-, 36- and 48- months' volatility period. Nevertheless, the results for 48-months volatility window turned out to work best and deliver the highest and significant positive alpha spread as well as Sharpe ratio (table 2 and 11 respectively). In line with the studies SMB and HML are insignificant for this asset class.

### REITs

For real-estate the factor loadings are also regressed on equal-weighted portfolios following the approach as for commodities. Table 2 shows the alpha spread for REITs sorted on 48 months volatility, however this turned out to be insignificant. Furthermore, Sharpe ratio for REIT is with negative coefficient (table 11). As a result, it can be summarized that low-volatility strategy does not work for this asset class.

### Multi-asset portfolio

It is noteworthy to explain that in the multi-asset portfolio, equities are being sorted on 12 months volatility period, investment grade bonds on 18 months, high-yield bonds on 18 months, commodities on 48 months and REITs on 48 months volatility windows. The multi-asset portfolio is built by taking the different volatility periods per asset class, as each asset class is sensitive to generate highest excess return for different volatility periods. Additionally, it is worth saying that other versions of volatility periods for the multi-asset portfolio were analyzed, however, the above mentioned tested volatility periods generated the highest excess return. Therefore, in the appendix only this unique version of the multi-asset portfolio is reported.

Table 2 and 11 also deliver the results for the multi-asset portfolio. SMB and HML are not significant as for the other asset classes. As it can be comprehended from table 2, positive and significant alpha spread with a coefficient of 0.387% means that low-volatility anomaly can be exploited for the multi-asset portfolio to deliver the highest excess return when compared to the individual asset classes. Also, table 11 proves that the multi-asset portfolio has generated the highest Sharpe ratio in comparison to the individual asset classes.

To summarize, referring to tables 2 and 11, the multi-asset portfolio generated the highest alpha spread (0.387) and the highest Sharpe ratio (0.029) when in comparison to individual asset classes. Equities sorted on 12 months and high- yield bonds sorted on 18 months volatility have the next highest alpha spreads and Sharpe ratios. Investment bonds and commodities perform worse on this investment strategy relative to the other assets by showing lower alpha spreads and Sharpe ratios. On the other hand, the low-volatility anomaly does not seem to work for REITs.

## **ii. Value effect**

### Equities

When constructing value factor for equities, a traditional sorting on the book-to-market ratio is applied. Consistent with the literature table 5 shows significant positive excess return when analyzed with Fama and French 3 factor model. Alpha spread (P5-P1) is also positive in respect to CAPM. Table 12 presents the Sharpe ratio from investing in this strategy (0.013) which is one of the highest in comparison to the other individual asset classes. Investing in value contributed to significant mispricing, therefore it can be exploited to generate substantial excess return.

For all other asset types than equities, the measures of value, attaining uniformity is more difficult because not all asset classes have a measure of book value. Therefore, the approach from Asness, et al., 2009, is used.

### Investment grade bonds

Following the methodology for the other asset classes outlined in the methodology part of the paper by Asness, et al, 2009, value impact on investment grade bonds is tested. Undesirably, table 5

shows that the generated alpha spread coefficient in investment bonds is insignificant. Besides, table 12 shows the lowest Sharpe ratio was achieved for this asset class. As a result, investing in value investment strategy for investment grade bonds is not beneficial. This outcome is in contrast with Houweling,2014. Perhaps a better approach to estimating value in investment grade bonds will support the outcome of Houweling, 2014.

### High yield bonds

Contrary to the result of investment grade bonds, high-yield bonds have proven to generate positive significant alpha spread. When compared to equities, the alpha spread of high-yield bonds is higher. In addition, the Sharpe ratio (table 12) is also higher than the one of equities. Consequently, it can be summarized that value effect generates excess return when investing in high yield bonds in line with Houweling, 2014.

### Commodities

As outlined in the methodology for commodities and real estate 'value is defined as the log of the spot price 5 years ago, divided by the most recent spot price, which is essentially the negative of the spot return over the last 5 years' (Asness, et al, 2009). These long-term past return measures of value are motivated by DeBondt and Thaler (1985) who use similar measures for individual stocks to identify "cheap" and "expensive" firms. Table 5 gives the results of testing value effect on commodities and shows that the alpha spread is insignificant . Furthermore, table 12 shows relatively low Sharpe ratio of 0.006, hence value effect cannot be exploited for this asset class.

### REITs

As explained in the above paragraph, reit follows the same methodology to construct the value factor as for commodities. Table 5 proves that value could be exploited for real-estate as the alpha spread is positive and significant. Also the Sharpe ratio for REIT is the highest in comparison to all individual asset classes and the multi-asset portfolio. This outcome is more than sufficient to conclude that a significant contribution of higher excess return of REITs is present due to exploiting the value factor.

### Multi-asset portfolio

Finally, multi-asset portfolio that consists of the 4 assets is being constructed with building value factor the same way as the other asset classes. Table 5 shows that value alpha spread is significant and positive. Also, the Sharpe ratio is positive and higher than the one for equities (table 12). However, the Sharpe ratio of REITs and high-yield bonds is higher than the one of the multi-asset portfolio. Consequently, it can be summarized that if perhaps REITs and high-yield bonds have higher weights than the currently 10%, the multi-asset portfolio would have probably generated the highest Sharpe ratio. However, for comparison reasons across all investment strategies, in this report only one multi-asset portfolio is being tested.

To recapitulate, REITs have shown the highest alpha spread (0.207) and the highest Sharpe ratio of 0.050, in reference with table 5 and 12. Second, high-yield bonds have produced the next highest Sharpe ratio of 0.033, followed by the multi-asset portfolio's one of 0.018. Third, equities have Sharpe ratio of 0.013 followed by commodities. Last, investment grade bonds have a negative Sharpe ratio and lowest alpha spread, while commodities have shown insignificant results, hence value strategy cannot be exploited for these two-asset class.

### **iii. The momentum impact**

#### Equities

With the aim of testing momentum effect per asset class, equal-weighted portfolios are constructed by sorting on past 6 and 12 months of cumulative returns, based on the CAPM and Fama and French 3 factor model. Table 8 reports the alpha spread for equities. When equities are sorted on 6 months cumulative returns, the outcome received is not significant with reference to CAPM. When looking at Fama and French 3 factor model's alpha spread, it is as well insignificant. Consequently, cumulative returns are sorted also on 12 months with the purpose to prove that this investment strategy works for this asset class. Table 8 also shows the results for equities sorted on 12 months cumulative returns and it can be seen that both CAPM alpha spread and Fama and French 3 factor model alpha-spread are significant. Table 13 presents the Sharpe ratios across the asset classes for momentum investment strategy. Sharpe ratio for equities sorted on 12 months is much higher than

the one of equities sorted on 6 months (0.140 vs. 0.002, respectively). For these portfolios, it can be concluded investing in size and value does not lead to significant risk premia for individual momentum quintile portfolios as SMB and HML coefficients are insignificant. For that reason, it can be established that the magnitude of mispricing in the U.S. with 12 months cumulative returns is in general consistent with existing literature, such as Jegadeesh and Titman (1993), as the constants are lower in the bottom quintile being past losers, and higher in the top quintile being past winners. In conclusion, sorting on cumulative returns of 12-months for equities delivers higher alpha and higher Sharpe ratio than when sorting portfolios on 6-months cumulative returns.

### Investment grade bonds

For investment grade bonds, table 8 shows the results for the portfolios that are formed on 12 months cumulative returns (CR). For portfolios formed on CR6 in the U.S. investment bonds market, the result was rather irrelevant, consequently only the alpha spread coefficients for CR12 months are reported. When compared to equities, investment grade bonds deliver lower alpha spread (table 8) and lower Sharpe ratio in comparison to equities sorted on 12 months CR, but higher Sharpe ratio than for equities sorted on CR6 (table 13). The significant and positive results that indicate excess return are in line with Houweling, 2014. Nevertheless, size premium (SMB) and value premium (HML) proved irrelevant when it comes to investment grade bonds.

### High-yield bonds

As cumulative returns of 6 months turn out to generate insignificant results, momentum strategy for high-yield bonds is tested also on 12 months cumulative returns. The results indicate lower alpha spread in comparison to investment grade bonds. From table 8 it can be interpreted that CAPM and Fama and French 3 factor alpha spread coefficients are positive and significant (Houweling, 2014). Table 13 reports the Sharpe ratio of high-yield investment bonds which is just slightly lower than the one of investment grade bonds (0.055 vs 0.056, respectively). Consistent with the conclusion for investment grade bonds, size and value premium did not contribute to any abnormal return.

### Commodities

Furthermore, momentum strategy tested on commodities on both CR6 and CR12 leads to inconsistent results in comparison with Asness, et al, 2009. The results of CR12 are slightly better

than these from the portfolios sorted on CR6, however still not beneficial (table 8). Table 13 reports the Sharpe ratio for this asset class of 0.003 which is rather low in comparison to the other asset classes. Therefore, momentum for commodities did not contribute positively to advantageous mispricing that potentially could be exploited.

### REITs

On the contrary of commodities results, momentum strategy leads to significant and positive abnormal return when testing on CAPM for both CR6 and CR12 sorting (table 8). Table 13 also shows the highest Sharpe ratio is for REITs (0.280) when compared to all other asset classes, which proves that momentum strategy could be taken advantage of for REITs. Alike effect is observed when examining cumulative returns on 6- and 12-months on Fama and French 3 factor model (table 8). As mentioned above SMB and HML are irrelevant with respect to commodities and real-estate. Consequently, for these portfolios it can be determined that investing in size and value does not lead to significant risk premia for individual momentum quintile portfolios. All in all, the real-estate market shows significant mispricing across quintile portfolios, regardless whether portfolios are formed on past 6 or 12 months CR, however sorting on CR12 generates slightly higher excess return and therefore only this result is reported in the tables. Therefore, one has noteworthy mispricing consistently throughout the dataset, therefore investing in up minus down momentum portfolios yields a significant abnormal return.

### Multi-asset portfolio

Last but not least, momentum investing strategy was tested on the multi-asset portfolio, consisting of 70% weight in equities, 10% in bonds portfolio (50% in high yield and 50% weight in investment grade bonds), 10% in commodities and 10% in real-estate. Table 8 shows the outcome of portfolios sorted on CR 12 for CAPM and Fama and French 3 factor model. When looking at Fama and French 3 factor model, SMB and HML are insignificant and indicate that there is not an advantageous size and value premium. When analyzing the alpha spread of P5-P1 ('winners' minus 'losers'), the result is significant and positive. Hence, momentum, with cumulative returns sorted on 12 months, leads to substantial mispricing and the multi-asset portfolio generates higher excess return, while at the same time it diversifies away the risk by investing in 4 different asset classes. All in all, the multi-asset portfolio outperforms the Sharpe ratios of some of the individual asset



classes such as equities sorted on 6 months cumulative returns, investment grade bonds, high-yield bonds and commodities.

To conclude, REITs have delivered the highest alpha spread (1.240) and the highest Sharpe ratio of 0.280, when referring to tables 8 and 13. Next, the multi-asset portfolio has generated the same Sharpe ratio as equities (0.140), both sorted on 12 months cumulative returns. Following, investment grade- and high-yield bonds have almost the same Sharpe ratios, with investment grade slightly higher. In addition, investment grade bonds show higher alpha spread relative to high-yield bonds. Last but not least, commodities sorted on 12 months CR and equities sorted on 6 months cumulative returns deliver the lowest excess returns.

## **Section VI: Robustness checks**

### **Low-volatility strategy**

First, the robustness of the results low-volatility strategy are examined to other cross-sectional factors. The regressions in this table are based on quintiles sorted on the same return volatility periods as described in the above mentioned section ‘Results-Low volatility strategy’, however in this case, time samples are taken into account. For all robustness checks the sample period is first analyzed for 1990-2007 and then for 2007-2015. 2007 year indicates the year that the financial crises has started, thus by splitting the time period in this way, the effect of financial crises on factor investment strategies could be exploited. This robustness check is done for all individual asset classes as well as for the multi-asset portfolio. When robustness check for low-volatility anomaly is tested, it can be concluded from tables 3 and 4 in the Appendix that high volatility portfolios perform worse than low volatility portfolios. These results indicate that the low volatility anomaly is robust for basing the return volatility on different time horizons. Furthermore, before the financial crises in 2007, every individual asset class delivers higher alpha spread for both CAPM and Fama and French 3 factor model in comparison to the after crises period 2007-2015. Hence, the excess return that is generated by investing in this factor strategy decreases due to the financial markets crash. The same observations can be drawn by look at table 11 that shows both pre-crisis Sharpe ratios and after crises Sharpe ratios. When the time horizon is split, higher Sharpe

ratios occur for pre-crises period. To conclude, persistent volatility effect is documented over time.

### **Value**

Contrary to the findings for low-volatility strategy, value strategy seems to actually perform slightly better in the after-crises period of 2007-2015. Tables 6 and 7 report the alpha spreads per individual assets and multi-asset portfolio, while table 12 presents the Sharpe ratios for both pre- and after- crises period. As it can be interpreted from the tables, only the multi-asset portfolio seems to generate slightly lower alpha spread in the post crises period and higher in the pre-crises period. All individual assets have generated higher alpha spread for the period 2007-2015. Consequently, based on the findings above it can be established that value investing strategy works the best for after crises period in comparison to low-volatility and momentum strategy.

### **Momentum**

In order to check whether the results for the momentum anomaly hold and are robust, subsamples are created for the same subperiods of 1990-2007 and 2008-2015 and examine whether each quintile presents a consistent alpha throughout the two periods. Tables 9,10 and 13 deliver the robustness check's results for this market anomaly. All constants are significant for the subsample 1990-2007 that suggests mispricing of the investigated asset classes. However, after 2007, the outburst of the recent financial crisis, only the high-yield bonds seem to have generated higher alpha after the financial crises in comparison to the pre-crises period. On the contrary, commodities seem to have fully crashed after the crises as the alpha spread becomes insignificant after the financial collapse in 2007. All in all, the U.S. market shows that it could not recover from this recession in terms of momentum yields.

## **Section VII: Concluding Remarks**

The global financial crises provided unexpected breakthrough, namely that many of the different asset classes have exposure to the same factors. Before the financial crises investors tended to allocate to assets instead of to factors which have led investors to have a high exposure to idiosyncratic risk, due to under diversification. Factor investing implementation was boosted due to the relatively recent financial crisis and it will remain in the long-term as an investment strategy

since numerous empirical studies have proved that it can be taken advantage of. In this paper, the strategies- low volatility, momentum, and value for the U.S. market were investigated. The aim of this study was to investigate the impact of these market anomalies on a multi-asset portfolio and to fill gaps in the financial literature. Some of the gaps in the existing arsenal of studies is that , studies are mainly focusing on individual asset classes. Therefore, this paper analyzes the impact of factors on a multi-asset portfolio. Furthermore, it investigates low-volatility effect on fixed-income market and also analyzes the impact of value, momentum and low-volatility on REITs, which has never been evaluated before. Additionally, it examines the most recent time period starting from January 1990 till December 2015.

For low-volatility strategy it can be summarized that the multi-asset portfolio has the highest alpha spread (0.387) and the highest Sharpe ratio (0.029) when in comparison to individual asset classes. Equities sorted on 12 months and high- yield bonds sorted on 18 months volatility have the next highest alpha spreads and Sharpe ratios. Investment bonds and commodities perform worse on this investment strategy relative to the other assets by showing lower alpha spreads and Sharpe ratios. In reference with the above paragraph, low-volatility strategy seems to work for the fixed-income market as well. On the other hand, the low-volatility anomaly does not seem to work for REITs.

When analyzing value effect, it can be recapitulated that REITs have shown the highest alpha spread (0.207) and the highest Sharpe ratio of 0.050. Second, high-yield bonds have produced the next highest Sharpe ratio of 0.033, followed by the multi-asset portfolio`s one of 0.018. Third, equities have Sharpe ratio of 0.013 followed by commodities. Last, investment grade bonds have a negative Sharpe ratio and lowest alpha spread, hence value strategy is not applicable for this asset class.

The results of momentum indicate that REITs have delivered the highest alpha spread (1.240) and the highest Sharpe ratio of 0.280. Next, the multi-asset portfolio has generated the same Sharpe ratio as equities (0.140), both sorted on 12 months cumulative returns. Following, investment grade- and high-yield bonds have almost the same Sharpe ratios, with investment grade slightly higher. In addition, investment grade bonds show higher alpha spread relative to high-yield bonds.

Last but not least, commodities sorted on 12 months CR and equities sorted on 6 months cumulative returns deliver the lowest excess returns.

From the performed analysis, conclusions can be drawn as well for the individual asset classes. Momentum in equities generates the highest Sharpe ratio, followed by low-volatility. For investment grade bonds and high yield bonds, momentum generates highest Sharpe ratio, however high yield bonds seems to have second best strategy value, while investment bonds's second best strategy would be low-volatility. For REIT, momentum seems to lead to the highest substantial excess return, followed by value investment strategy. On the contrary, commodities seem to generate highest excess return when low-volatility strategy is being applied. Last but not least, the multi-asset portfolio has generated highest Sharpe ratio when momentum investing is used, followed by low-volatility and value strategies.

Some limitations of this study should also be considered. First, transaction costs are not considered in this report. Second, the conclusions are based on selected benchmark asset pricing models. Further research could be conducted by utilizing other asset pricing models such as the Fama and French (2015) 5 factor model. Third, the results obtained in this paper may not be valid for other markets, because the features of each market vary. Fourth, this study was utilizing quintile portfolios, hence another approach would be to rather use deciles, to stretch out the variation within the data. Last, the research of this paper could be extended for other developed markets, as well as, for developing markets.

These research findings will present a challenge to existing rational, behavioral and institutional asset pricing theories that mainly focus on U.S. equities. This paper could be of interest to leading asset management companies and investors who would like to maximize returns by better portfolio diversification achieved by combining multi assets and taking advantage of exploiting market anomalies as investment strategies.

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## Appendix

**Table 1:** The table depicts summary statistics, including mean, standard deviation (sd), minimum value (min) and maximum (max) value for selected variables. The period covers 1990-2015.

Variables	(1) N	(2) mean	(3) sd	(4) min	(5) max
Time	2,120,237	557.314	115.872	366	798
Excess Return Equities	935,896	0.275	601.448	-577.650	49,100
SMB	1,765,320	0.133	3.274	-17.170	22.080
HML	1,765,320	0.207	3.009	-11.250	12.910
Risk-free Rate	1,765,320	0.584	4.334	-17.230	11.350
ID	2,120,237	3,057.424	1,614.951	1	5,669
Date	2,120,237	16,184.510	2,772.857	10,958	20,454
Year	2,120,237	2,003.855	7.589	1990	2016
Month	2,120,237	6.485	3.459	1	12
Yield Investment Bonds	2,120,237	0.001	0.016	-0.070	0.056
Price Investment Bonds	2,120,237	103.665	5.501	83.718	115.14
Price High Yield Bonds	2,120,237	92.026	13.769	0	106.768
Yield High Yield Bonds	2,091,892	0.001	0.028	-0.169	0.132
Commodities Price	2,120,237	103.665	5.501	83.718	115.140
REITs Return	2,120,237	0.927	5.441	-29.852	33.721
Commodities Return	2,120,237	0.018	1.592	-7.000	5.569
Commodities Excess Return	1,765,320	-0.218	1.573	-7.150	5.569
REITs Excess Return	1,765,320	0.743	5.099	-29.932	33.711

**Table 2: Low-volatility strategy.** Equal-weighted quintile portfolios are created each month by sorting assets on different volatility periods. The volatility periods vary from 6 months to 48 months per asset class, indicated next to the asset name in each column. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) volatility period. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied. The sample period is January 1990 to December 2015.

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
Dependent Variable	Spread Equities 6m	Spread Equities 12m	Spread Investment Bonds 12m	Spread Investment Bonds 18m	Spread High-Yield Bonds 12m	Spread High-Yield Bonds 18m	Spread Commodities 24m	Spread Commodities 48m	Spread REITs 48m	Spread MA portfolio
Alpha CAPM	0.278*** (0.065)	0.323*** (0.069)	0.052** (0.023)	0.067*** (0.020)	0.042 (0.035)	0.027 (0.027)	0.043 (0.017)	0.065*** (0.015)	-0.055 (0.033)	0.365*** (0.046)
Observations	313	313	313	313	313	313	313	313	313	313
R-squared	0.01	0.01	0.02	0.01	0.01	0.01	0.04	0.05	0.01	0.01
Alpha FF3	0.267*** (0.065)	0.309*** (0.070)	0.057* (0.023)	0.070* (0.021)	0.051 (0.036)	0.267*** (0.065)	0.043*** (0.016)	0.066*** (0.016)	-0.031 (0.030)	0.387*** (0.084)
SMB	0.035 (0.026)	0.049 (0.029)	-0.009 (0.007)	-0.007 (0.006)	-0.032 (0.013)	0.034 (0.026)	0.007 (0.005)	0.005 (0.005)	-0.062 (0.010)	-0.050 (0.036)
HML	0.037 (0.032)	0.041 (0.036)	-0.019** (0.009)	-0.010 (0.008)	-0.026 (0.017)	0.037 (0.032)	-0.002 (0.006)	-0.003 (0.005)	-0.079 (0.011)	-0.077 (0.034)
Observations	313	313	313	313	313	313	313	313	313	313
R-squared	0.02	0.02	0.02	0.01	0.04	0.02	0.04	0.05	0.01	0.07

Robust standard errors in parentheses

\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 3: Robustness check 1990-2007. Low-volatility strategy.** The table presents the results for the period 1990-2007. Equal-weighted quintile portfolios are created each month by sorting assets on different volatility periods. The volatility periods vary from 6 months to 48 months per asset class, indicated next to the asset in each column. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) volatility period. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied.

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
<b>1990-2007</b>	Spread	Spread	Spread	Spread	Spread	Spread	Spread	Spread	Spread	Spread
<b>Dependent Variable</b>	Equities 6m	Equities 12m	Investment Bonds 12m	Investment Bonds 18m	High-Yield Bonds 12m	High-Yield Bonds 18m	Commodities 24m	Commodities 48m	REITs 48m	Spread MA portfolio
Alpha CAPM	0.264*** (0.058)	0.316*** (0.071)	0.070** (0.030)	0.090*** (0.028)	0.042 (0.375)	0.030 (0.422)	0.068*** (0.023)	0.093*** (0.022)	0.097** (0.048)	0.192*** (0.041)
Observations	205	205	205	205	205	205	205	205	205	205
R-squared	0.01	0.01	0.01	0.01	0.02	0.01	0.05	0.04	0.05	0.01
Alpha FF3	0.211*** (0.051)	0.252*** (0.063)	0.088*** (0.031)	0.102*** (0.029)	0.071 (0.051)	0.052 (0.041)	0.076*** (0.024)	0.105*** (0.024)	0.012 (0.044)	0.173*** (0.038)
SMB	0.048* (0.025)	0.065** (0.030)	-0.012 (0.008)	-0.009 (0.008)	-0.038** (0.016)	-0.022* (0.013)	0.004 (0.007)	0.001 (0.006)	-0.083 (0.013)	0.018 (0.330)
HML	0.074** (0.029)	0.090** (0.036)	-0.026** (0.012)	-0.018* (0.011)	-0.041* (0.024)	-0.031* (0.018)	-0.013 (0.008)	-0.019 (0.008)	-0.121 (0.016)	0.028 (0.183)
Observations	205	205	205	205	205	205	205	205	205	205
R-squared	0.07	0.08	0.03	0.02	0.05	0.03	0.06	0.07	0.03	0.02

Robust standard errors in parentheses

\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 4: Robustness check 2007-2015. Low-volatility strategy.** The table presents the results for the period 2007-2015. Equal-weighted quintile portfolios are created each month by sorting assets on different volatility periods. The volatility periods vary from 6 months to 48 months per asset class, indicated next to the asset in each column. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) volatility period. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied.

	Spread	Spread	Spread	Spread	Spread	Spread	Spread	Spread	Spread	Spread
<b>2007-2015</b>	Equities 6m	Equities 12m	Investment Bonds 12m	Investment Bonds 18m	High-Yield Bonds 12m	High-Yield Bonds 18m	Commodities 24m	Commodities 48m	REITs 48m	Spread MA portfolio
Alpha CAPM	0.309** (0.150)	0.336** (0.151)	0.015 (0.029)	0.023 (0.024)	0.038 (0.053)	0.020 (0.037)	0.002 (0.015)	0.014 (0.014)	0.023 (0.031)	0.210** (0.103)
Observations	108	108	108	108	108	108	108	108	108	108
R-squared	0.01	0.03	0.04	0.02	0.04	0.03	0.06	0.09	0.01	0.01
Alpha FF3	0.302** (0.0149)	0.327** (0.148)	0.012 (0.030)	0.023 (0.023)	0.042 (0.052)	0.025 (0.036)	0.002 (0.015)	0.018 (0.015)	0.010 (0.028)	0.211** (0.102)
SMB	0.032 (0.074)	0.051 (0.074)	-0.003 (0.015)	-0.007 (0.010)	-0.024 (0.028)	-0.008 (0.021)	0.005 (0.006)	0.004 (0.005)	-0.016 (0.013)	0.022 (0.051)
HML	0.020 (0.074)	0.031 (0.073)	-0.008 (0.015)	0.002 (0.013)	0.014 (0.029)	0.015 (0.021)	-0.001 (0.005)	0.013 (0.006)	-0.037 (0.012)	-0.013 (0.049)
Observations	108	108	108	108	108	108	108	108	108	108
R-squared	0.01	0.01	0.05	0.02	0.06	0.04	0.04	0.02	0.01	0.01

Robust standard errors in parentheses

\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 5: Value strategy.** Equal-weighted quintile portfolios are created each month by sorting assets on their value. Value for equities is calculated by taking the book-to-market ratio, while for all other assets a standardized approach is applied. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) value. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied. The sample period is January 1990 to December 2015.

	(1)	(2)	(3)	(4)	(5)	(6)
Dependent Variable	Spread Equities	Spread Investment Bonds	Spread High-Yield Bonds	Spread Commodities	Spread REITs	Spread MA portfolio
Alpha CAPM	0.117** (0.028)	0.314 (0.016)	0.165*** (0.049)	0.049 (0.031)	0.207** (0.064)	0.187*** (0.062)
Observations	313	313	313	313	313	247
R-squared	0.01	0.01	0.01	0.02	0.01	0.01
Alpha FF3	0.119*** (0.028)	0.007 (0.019)	0.164** (0.051)	0.048 (0.033)	0.207** (0.066)	0.189*** (0.020)
SMB	-0.013 (0.010)	0.006 (0.005)	-0.002 (0.015)	0.003 (0.012)	0.013 (0.019)	-0.003 (0.006)
HML	-0.006 (0.010)	0.004 (0.005)	-0.004** (0.013)	-0.001 (0.014)	-0.001 (0.026)	-0.004 (0.006)
Observations	313	313	313	313	313	247
R-squared	0.01	0.01	0.01	0.02	0.02	0.01

Robust standard errors in parentheses

\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 6: Robustness check 1990-2007. Value strategy.** The table presents the results for the sample of 1990-2007. Equal-weighted quintile portfolios are created each month by sorting assets on their value. Value for equities is calculated by taking the book-to-market ratio, while for all other assets a standardized approach is applied. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) value. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied.

	(1)	(2)	(3)	(4)	(5)	(6)
1990-2007 Dependent Variable	Spread Equities	Spread Investment Bonds	Spread High-Yield Bonds	Spread Commodities	Spread REITs	Spread MA portfolio
Alpha CAPM	0.065** (0.032)	0.065** (0.029)	0.125** (0.053)	0.076** (0.032)	0.167** (0.076)	0.188*** (0.032)
Observations	205	205	205	205	205	205
R-squared	0.01	0.03	0.01	0.01	0.03	0.01
Alpha FF3	0.062** (0.031)	0.075** (0.031)	0.112* (0.058)	0.085* (0.031)	0.166** (0.077)	0.192*** (0.034)
SMB	0.006 (0.011)	-0.023 (0.009)	0.004 (0.017)	-0.003 (0.014)	-0.017 (0.018)	-0.002 (0.008)
HML	-0.005 (0.012)	-0.130 (0.011)	0.020 (0.017)	0.014 (0.016)	-0.001 (0.031)	-0.005 (0.011)
Observations	205	205	205	205	205	205
R-squared	0.01	0.06	0.01	0.01	0.02	0.01

Robust standard errors in parentheses

\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 7: Robustness check 2007-2015. Value strategy.** The table presents the results for the sample of 2007-2015. Equal-weighted quintile portfolios are created each month by sorting assets on their value. Value for equities is calculated by taking the book-to-market ratio, while for all other assets a standardized approach is applied. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) value. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied.

	(1)	(2)	(3)	(4)	(5)	(6)
<b>2007-2015</b> Dependent Variable	Spread Equities	Spread Investment Bonds	Spread High-Yield Bonds	Spread Commodities	Spread REITs	Spread MA portfolio
Alpha CAPM	0.213*** (0.054)	0.127** (0.056)	0.235** (0.099)	0.235** (0.123)	0.289** (0.123)	0.186*** (0.037)
Observations	108	108	108	108	108	108
R-squared	0.01	0.02	0.02	0.01	0.01	0.01
Alpha FF3	0.210*** (0.052)	0.130** (0.058)	0.241** (0.102)	0.001 (0.067)	0.281** (0.127)	0.186*** (0.037)
SMB	0.037 (0.023)	0.017 (0.025)	-0.009 (0.053)	0.016 (0.035)	0.002 (0.049)	-0.015 (0.014)
HML	0.006 (0.018)	0.009 (0.026)	0.017 (0.036)	0.003 (0.024)	0.024 (0.047)	-0.001 (0.016)
Observations	108	108	108	108	108	108
R-squared	0.02	0.02	0.02	0.05	0.01	0.02

Robust standard errors in parentheses

\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 8: Momentum strategy.** Equal-weighted quintile portfolios are created each month by sorting assets on their cumulative returns (either on 6 months cumulative return or on 12 months. Next to the asset name in each column, the cumulative returns period is specified. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) cumulative returns. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied. The sample period is January 1990 to December 2015.

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
Dependent Variable	Spread Equities 6m	Spread Equities 12m	Spread Investment Bonds 12m	Spread High-Yield Bonds 12m	Spread Commodities 12m	Spread REITs 12m	Spread MA portfolio 6m	Spread MA portfolio 12m
Alpha CAPM	0.023 (0.367)	1.030*** (0.326)	0.539** (0.114)	0.470*** (0.135)	0.027 (0.019)	1.230*** (0.024)	0.067 (0.247)	0.918** (0.307)
Observations	307	307	313	313	313	313	313	296
R-squared	0.01	0.02	0.01	0.01	0.01	0.01	0.01	0.01
Alpha FF3	0.039 (0.364)	1.120*** (0.315)	0.545*** (0.117)	0.465*** (0.139)	0.026 (0.019)	1.240*** (0.024)	0.097 (0.250)	1.000*** (0.296)
SMB	-0.107 (0.164)	-0.053 (0.140)	0.048 (0.045)	-0.024 (0.044)	-0.007 (0.008)	-0.011 (0.008)	-0.060 (0.099)	-0.038 (0.133)
HML	-0.185 (0.201)	-0.255 (0.165)	-0.029 (0.049)	0.010 (0.058)	0.002 (0.007)	-0.004 (0.008)	-0.100 (0.126)	-0.236 (0.160)
Observations	307	307	313	313	313	313	313	296
R-squared	0.01	0.02	0.02	0.01	0.01	0.01	0.01	0.02

Robust standard errors in parentheses

\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 9: Robustness check 1990-2007. Momentum strategy.** The table reports the results for the sample 1990-2007. Equal-weighted quintile portfolios are created each month by sorting assets on their cumulative returns (either on 6 months cumulative return or on 12 months. Next to the asset name in each column, the cumulative returns period is specified. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) cumulative returns. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied.

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
<b>1990-2007</b> Dependent Variable	Spread Equities 6m	Spread Equities 12m	Spread Investment Bonds 12m	Spread High-Yield Bonds 12m	Spread Commodities 12m	Spread REITs 12m	Spread MA portfolio 6m	Spread MA portfolio 12m
Alpha CAPM	0.104 (0.434)	1.130*** (0.422)	0.536*** (0.139)	0.434*** (0.158)	0.046** (0.022)	1.230*** (0.029)	0.002 (0.292)	1.040*** (0.393)
Observations	204	204	204	204	204	204	204	204
R-squared	0.01	0.01	0.02	0.01	0.01	0.01	0.01	0.01
Alpha FF3	0.226 (0.367)	1.560*** (0.352)	0.546*** (0.144)	0.423*** (0.161)	0.045** (0.023)	1.240*** (0.031)	0.185 (0.271)	1.440*** (0.321)
SMB	-0.224 (0.174)	-0.169 (0.153)	0.061 (0.051)	-0.024 (0.050)	-0.008 (0.008)	0.007 (0.009)	-0.131 (0.107)	-0.154 (0.144)
HML	-0.431 (0.219)	-0.506 (0.199)	-0.021 (0.057)	0.018 (0.069)	0.002 (0.007)	-0.008 (0.012)	-0.271 (0.135)	-0.473 (0.193)
Observations	204	204	204	204	204	204	204	204
R-squared	0.05	0.06	0.03	0.01	0.01	0.01	0.03	0.07

Robust standard errors in parentheses  
\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 10: Robustness check 2007-2015. Momentum strategy.** The table reports the results for the sample 2007-2015. Equal-weighted quintile portfolios are created each month by sorting assets on their cumulative returns (either on 6 months cumulative return or on 12 months. Next to the asset name in each column, the cumulative returns period is specified. In each column, the spread of P5 - P1 is reported, with P1 (P5) is the portfolio of stocks with the lowest (highest) cumulative returns. Jensen's alpha with respect to the CAPM and Fama & French 3 factor model. Robust Newey-West (1987) standard errors are always applied.

	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
<b>2007-2015</b> Dependent Variable	Spread Equities 6m	Spread Equities 12m	Spread Investment Bonds 12m	Spread High-Yield Bonds 12m	Spread Commodities 12m	Spread REITs 12m	Spread MA portfolio 6m	Spread MA portfolio 12m
Alpha CAPM	0.109 (0.687)	0.823 (0.535)	0.527** (0.196)	0.521*** (0.252)	0.011 (0.036)	1.240*** (0.041)	0.195 (0.461)	0.681** (0.506)
Observations	109	109	109	109	109	109	109	109
R-squared	0.01	0.01	0.01	0.01	0.02	0.01	0.01	0.01
Alpha FF3	0.183 (0.652)	0.855 (0.535)	0.547*** (0.193)	0.543** (0.247)	-0.007 (0.036)	1.230*** (0.042)	0.252 (0.447)	0.719 (0.501)
SMB	0.085 (0.366)	0.086 (0.305)	0.012 (0.097)	-0.015 (0.134)	-0.003 (0.016)	0.032 (0.022)	0.024 (0.238)	0.127 (0.299)
HML	0.210 (0.232)	0.087 (0.254)	0.062 (0.096)	0.067 (0.105)	0.011 (0.013)	0.010 (0.015)	0.165 (0.233)	0.100 (0.236)
Observations	109	109	109	109	109	109	109	109
R-squared	0.01	0.01	0.02	0.01	0.02	0.03	0.01	0.02

Robust standard errors in parentheses  
\*\*\* p<0.01, \*\* p<0.05, \* p<0.1

**Table 11:** The table depicts Sharpe Ratios for Low-Volatility Investment Strategy for selected portfolios. The spread portfolio represents the spread of P5 - P1, with P1 (P5) is the portfolio of stocks with the lowest (highest) volatility period. Multi-asset portfolio is constructed based on 12m volatility period for equities, 18m for bonds and 48m volatility period for commodities and REITs. The period covers 1990-2015. Column (2) and (3) report the Sharpe ratios per selected time periods (1990-2007, 2007-2015) with the purpose of robustness check.

Portfolios	(1) Sharpe Ratio	(2) Sharpe Ratio 1990-2007	(3) Sharpe Ratio 2007-2015
Equities 6m	0.023	0.032	0.016
Equities 12m	0.027	0.038	0.017
Investment Bonds 12m	0.004	0.009	0.001
Investment Bonds 18m	0.006	0.011	0.001
High-yield Bonds 12m	0.003	0.005	0.001
High-yield Bonds 18m	0.024	0.004	0.001
Commodities 24m	0.003	0.007	-0.003
Commodities 48m	0.005	0.009	0.001
REIT 48m	-0.007	-0.015	-0.001
MA Portfolio	0.029	0.023	0.011

**Table 12:** The table depicts Sharpe Ratios for Value Investment Strategy for selected portfolios. The spread portfolio represents the spread of P5 - P1, with P1 (P5) is the portfolio of stocks with the lowest (highest) value. The period covers 1990-2015. Column (2) and (3) report the Sharpe ratios per selected time periods (1990-2007, 2007-2015) with the purpose of robustness check.

Portfolios	(1) Sharpe Ratio	(2) Sharpe Ratio 1990-2007	(3) Sharpe Ratio 2007-2015
Equities	0.013	0.008	0.017
Investment Bonds	0.001	0.007	0.009
High-yield Bonds	0.033	0.030	0.034
Commodities	0.006	-0.018	0.005
REIT	0.050	-0.037	0.056
MA Portfolio	0.018	0.042	0.037

**Table 13:** The table depicts Sharpe Ratios for Momentum Investment Strategy for selected portfolios. The spread portfolio represents 'winners'-losers' portfolios (P5-P1). 6m and 12m indicate the period on what period of cumulative returns a particular asset is sorted. The period covers 1990-2015. Column (2) and (3) report the Sharpe ratios per selected time periods (1990-2007, 2007-2015) with the purpose of robustness check.

Portfolios	(1) Sharpe Ratio	(2) Sharpe Ratio 1990-2007	(3) Sharpe Ratio 2007-2015
Equities 6m	0.002	-0.006	0.013
Equities 12m	0.140	0.176	0.103
Investment Bonds 12m	0.056	0.065	0.046
High-yield Bonds 12m	0.055	0.051	0.054
Commodities 12m	0.003	0.006	-0.001
REIT 12m	0.280	0.296	0.263
MA Portfolio 12m	0.140	0.175	0.086